

# Retrieving LWC from Zenith-Pointing Microwave Observations (NOT)

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# Information Content

- Most retrieval problems are ill-defined
- Retrieval technique must add information to constrain the retrieved state vector  $\mathbf{X}$  (i.e., the solution)
- Important to know how much of the information in  $\mathbf{X}$  is from the observations vs. from the retrieval technique
- Some methods, such as optimal estimation, allow this to be determined directly

# Optimal Estimation

State Vector      Jacobian      Observations      Forward Calc  $y_i = f(X_i)$

$$\mathbf{x}_{i+1} = \mathbf{x}_i + \left( \mathbf{K}_i^T \mathbf{S}_e^{-1} \mathbf{K}_i + \mathbf{S}_a^{-1} \right)^{-1} \left[ \mathbf{K}_i^T \mathbf{S}_e^{-1} (\mathbf{y} - \mathbf{y}_i) + \mathbf{S}_a^{-1} (\mathbf{x}_a - \mathbf{x}_i) \right]$$

Measurement Covariance Matrix      A Priori Covariance Matrix      A Priori State Vector

“Optimal” Solution Covariance Matrix

$$\mathbf{S}_{op} = \left( \mathbf{K}_i^T \mathbf{S}_e^{-1} \mathbf{K}_i + \mathbf{S}_a^{-1} \right)^{-1}$$

Averaging Kernal

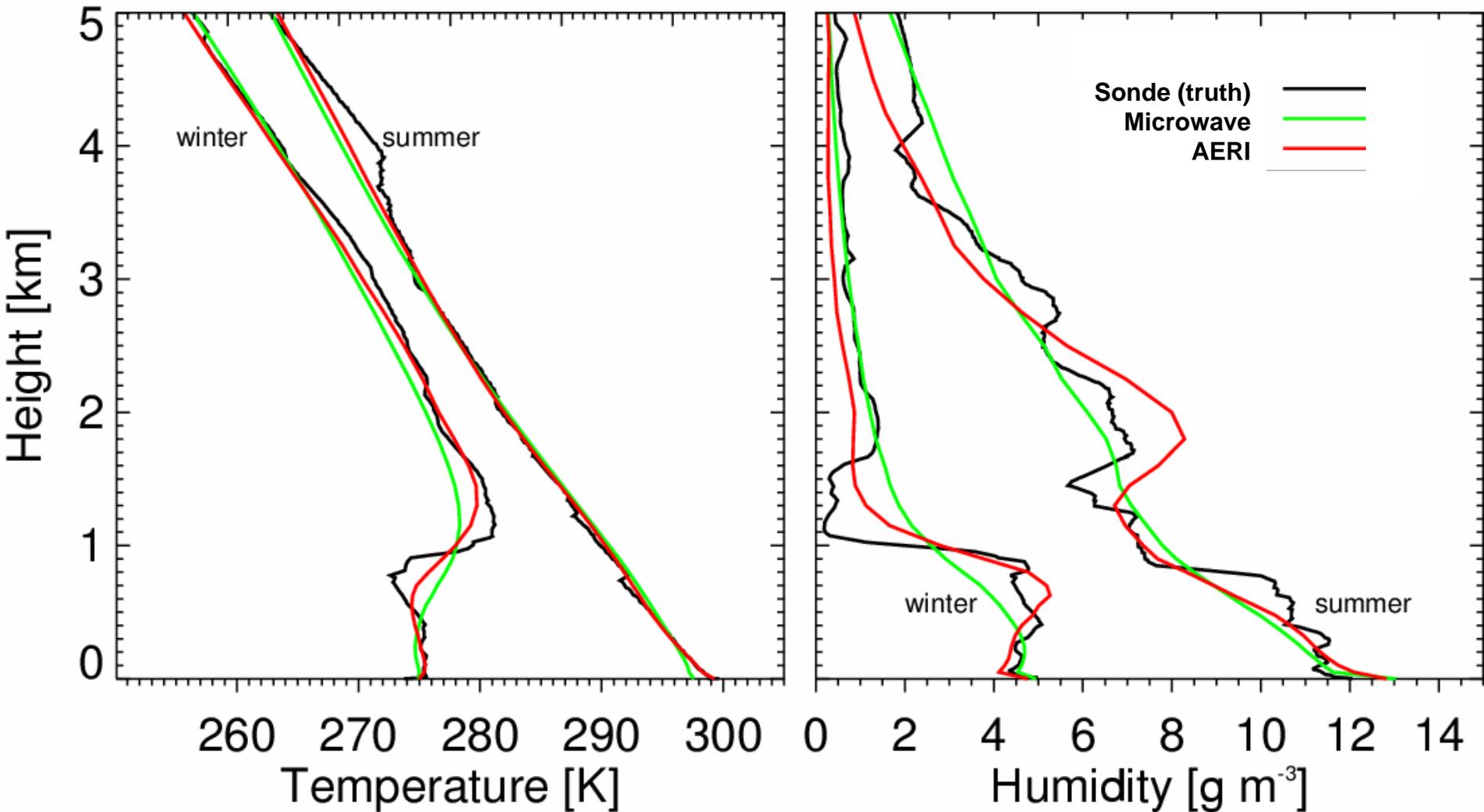
$$\mathbf{A} = \mathbf{S}_{op} \cdot \left( \mathbf{K}_{op}^T \mathbf{S}_e^{-1} \mathbf{K}_{op} \right)$$

Trace(A) = Degrees of Freedom of Signal

# Retrieving Water Vapor and Temperature Profiles

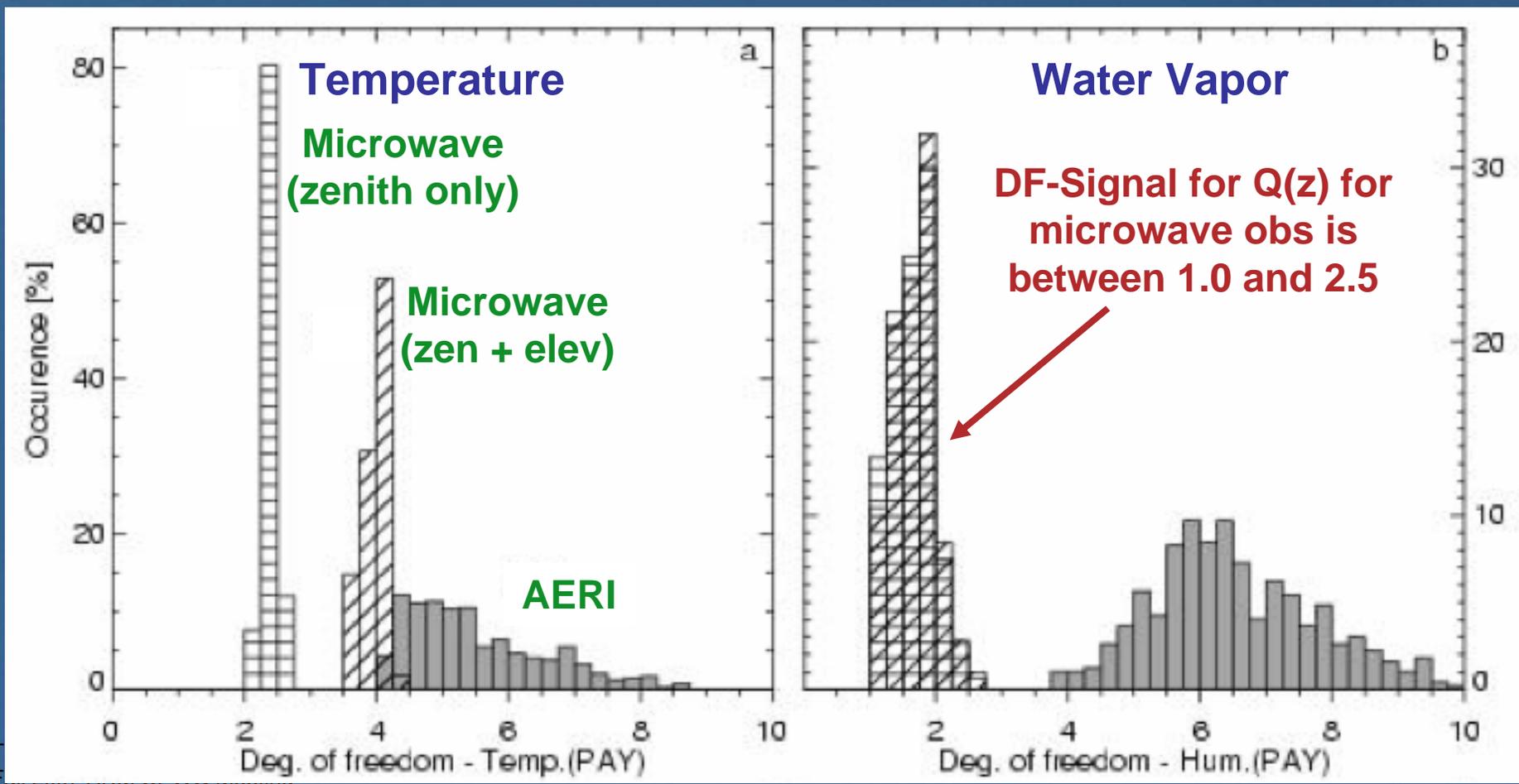
- Multi-channel microwave radiometers have been used to profile T and Q
- Typically use observations on side of 22.2 GHz H<sub>2</sub>O line and 60 GHz O<sub>2</sub> complex
- Due to transparency of non-precipitating clouds in microwave, T/Q profiles can be retrieved the majority of the time
- Also able to retrieve T/Q profiles from AERI, but clouds can be very limiting
- What is the information content (i.e., number of pieces of independent information) for T/Q profiles in these observations?

# Example: Retrieved T/Q Profiles in Clear Sky Mid-Latitude Conditions



# Distribution of Degrees of Freedom of Signal for Retrieved T/Q Profiles

Mid-latitude site, several hundred clear-sky examples spanning range of PWV

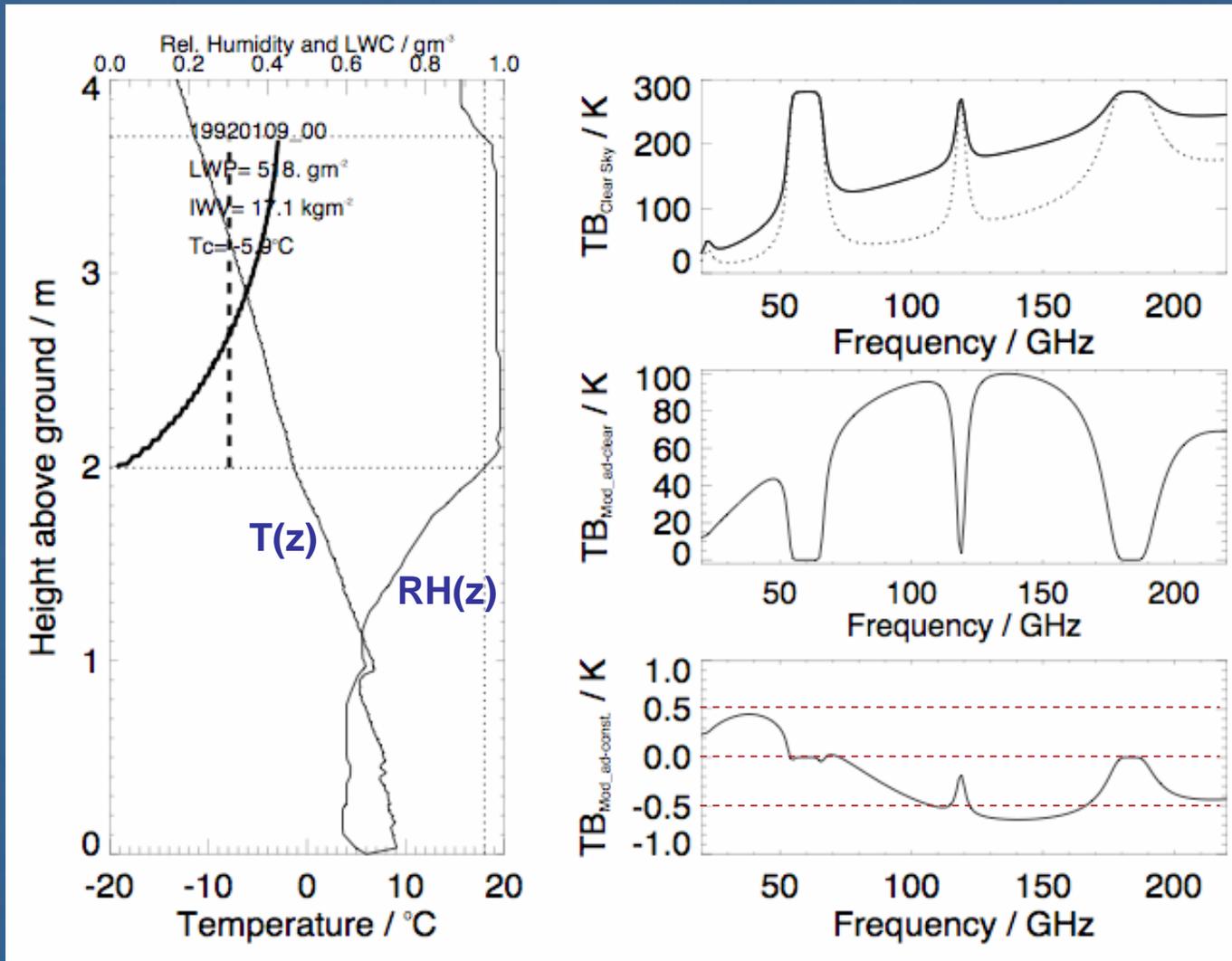


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- Some methods, such as optimal estimation, allow this to be determined directly
- Question: How much information content is there in passive zenith microwave radiometer observations to the profile of LWC?

# Sensitivity of Microwave Obs to LWC(z)

## Thick Cloud – 518 g/m<sup>2</sup>



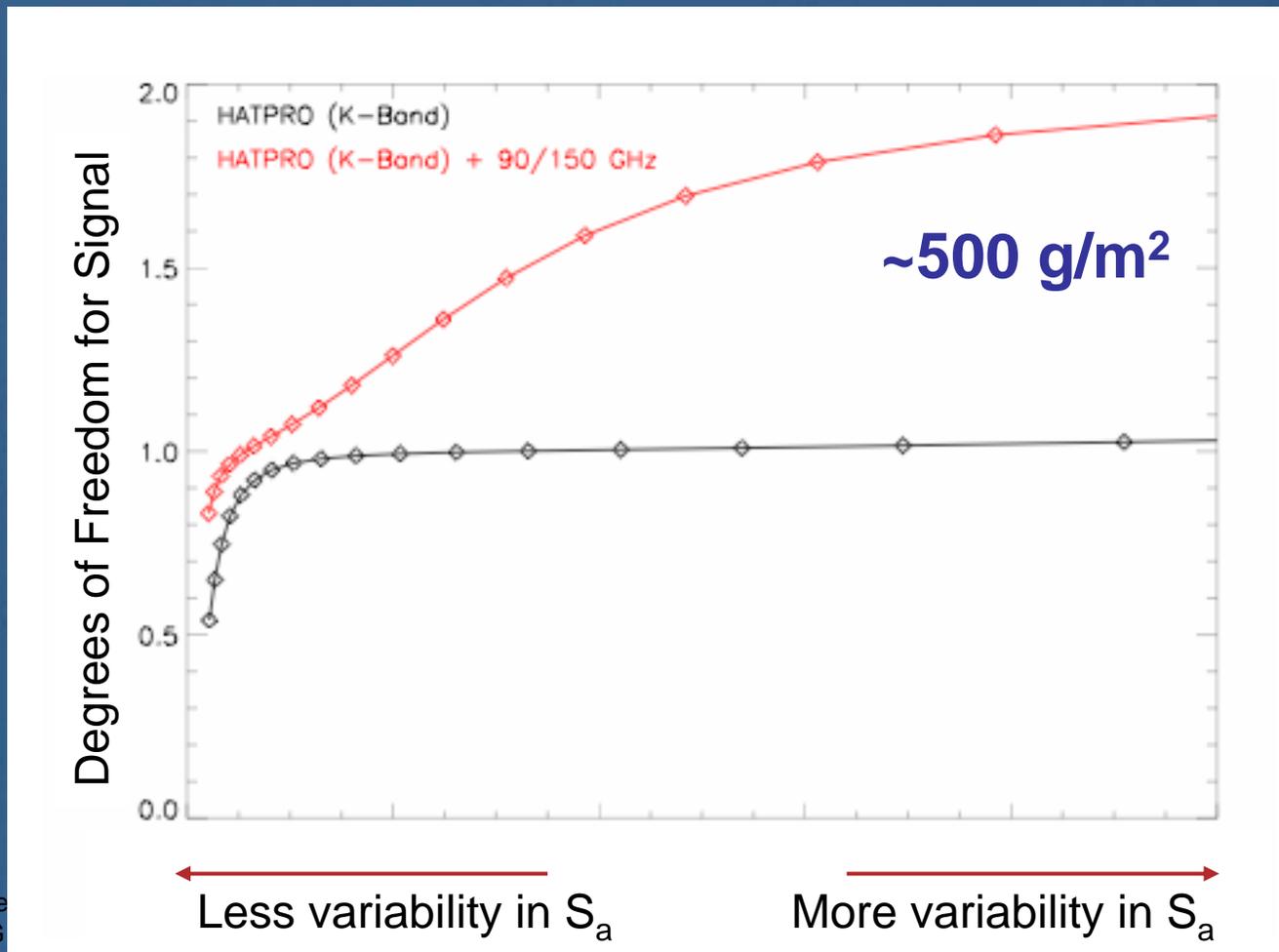
Cloudy T<sub>b</sub>  
Clear T<sub>b</sub>

Cloud  
minus  
Clear

Sub-adiabatic  
minus  
Constant  
LWC(z)

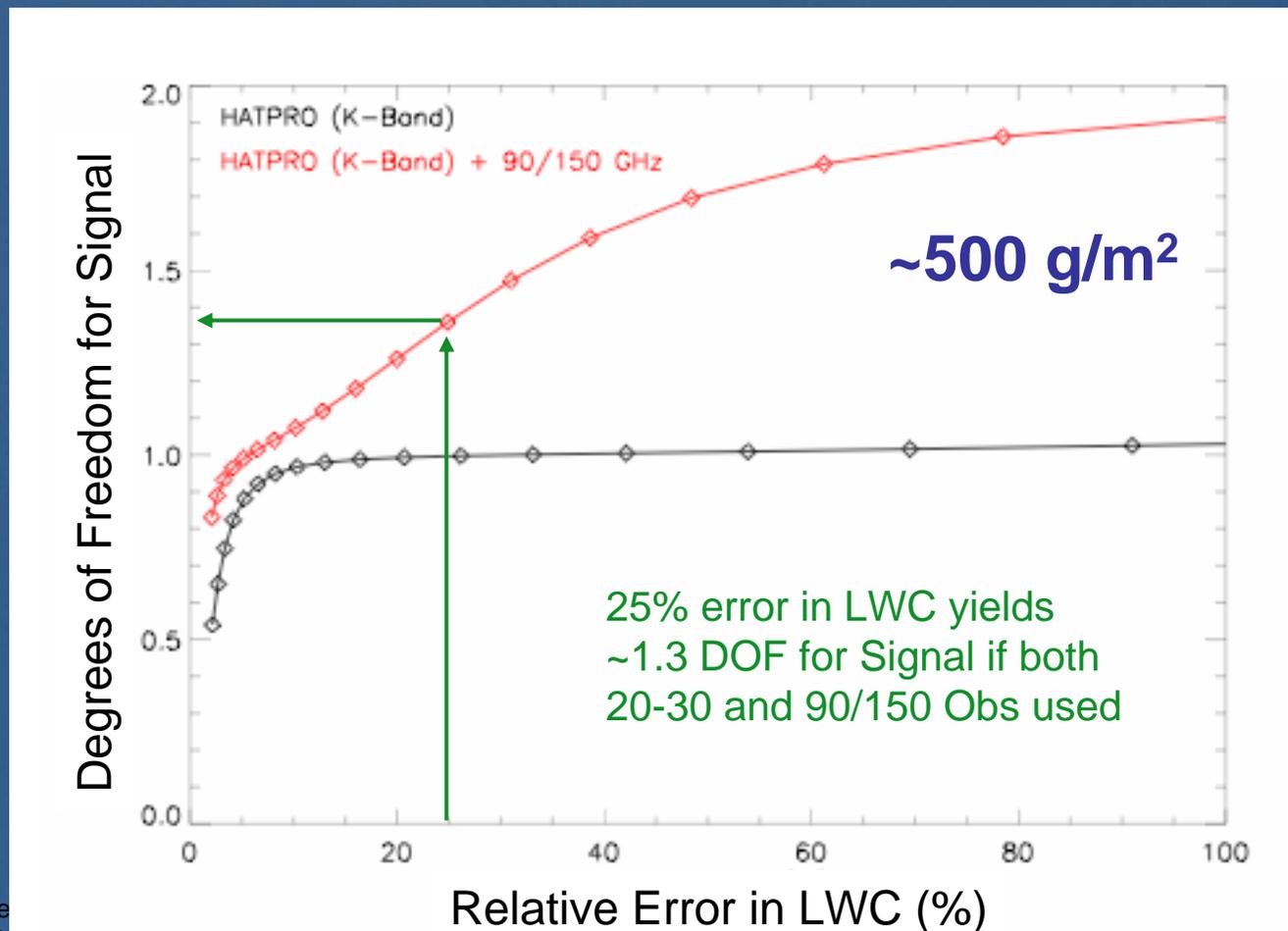
# Sensitivity to A Priori Information

- Less variability in climatology covariance matrix ( $S_a$ ) will constrain the solution close to the a priori  $X_a$ 
  - Results in less degrees of freedom in signal

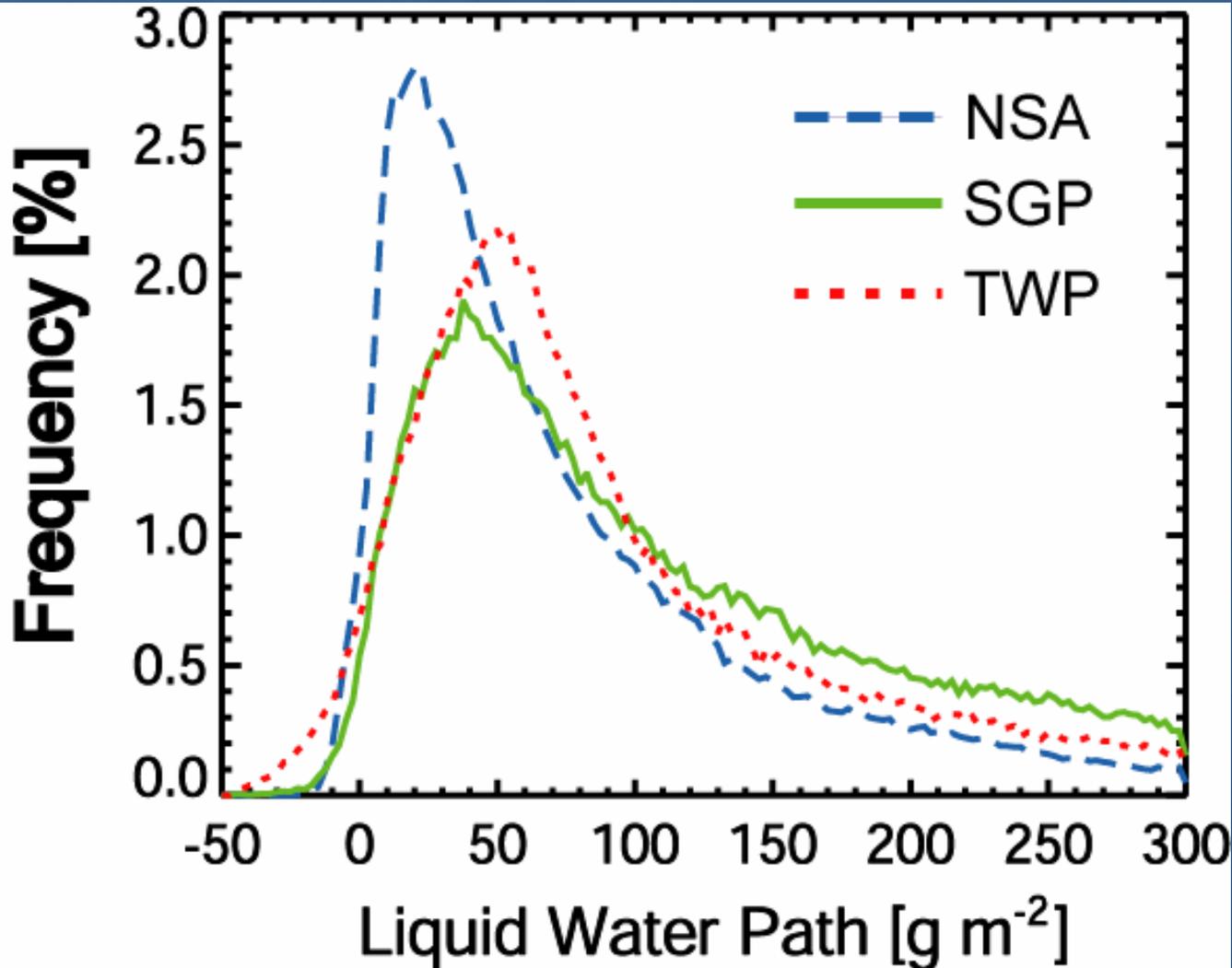


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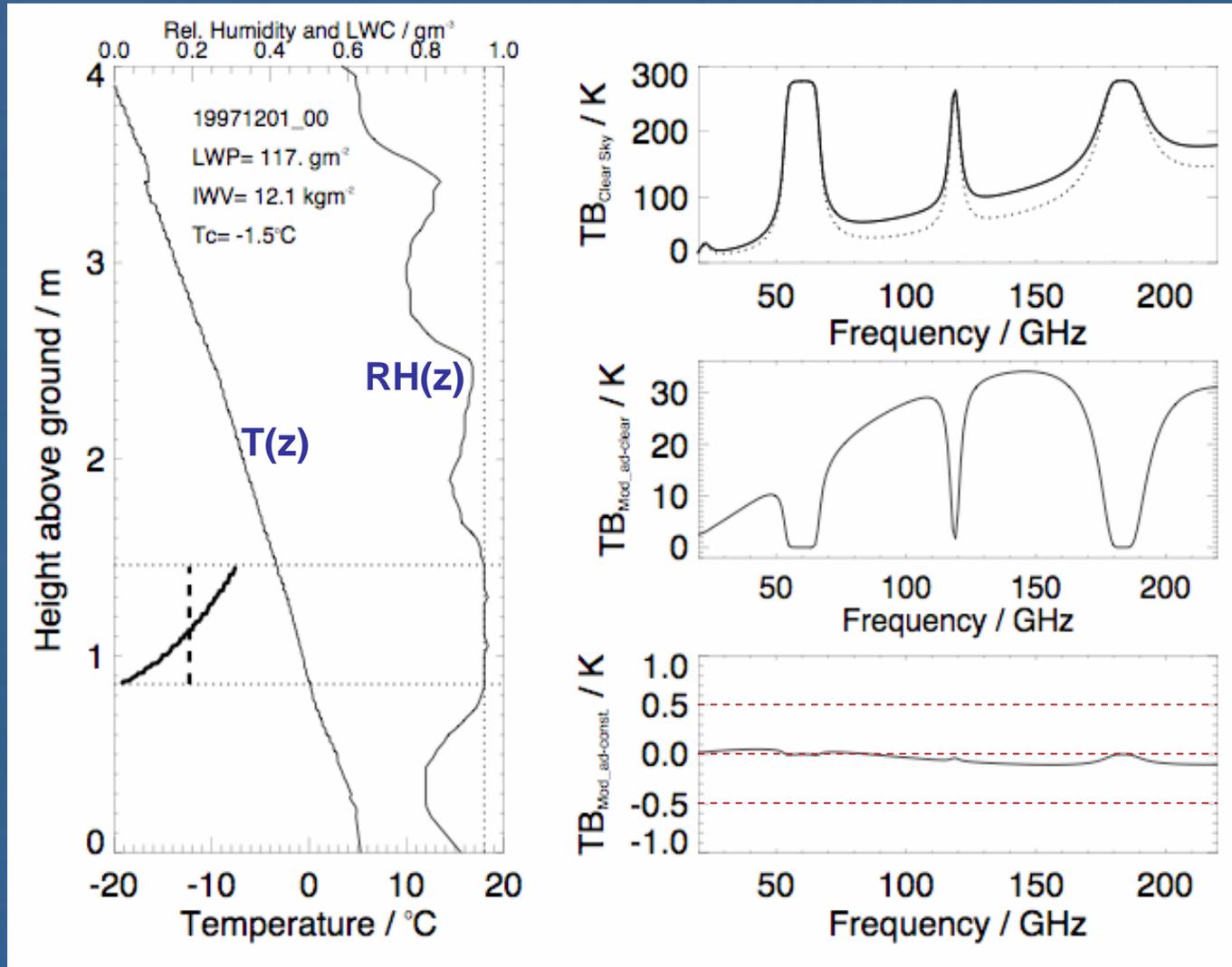
# Distribution of LWP at ARM Sites



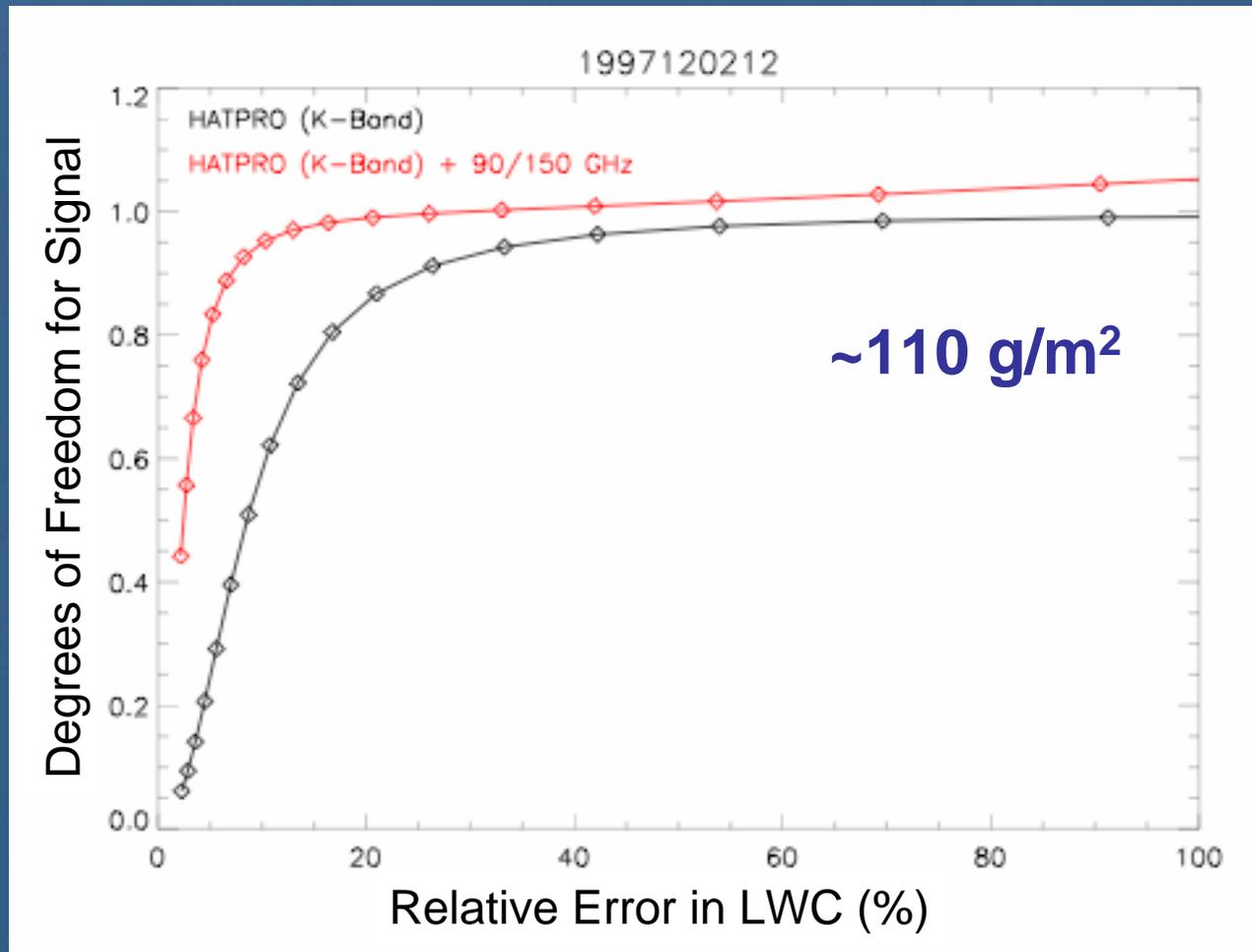
Most clouds have  
LWP  $\ll$  200  $\text{g m}^{-2}$

# Sensitivity of Microwave Obs to LWC(z)

## Thinner Cloud – 117 g/m<sup>2</sup>



# DoF Signal for LWC(z) in Thin Cld

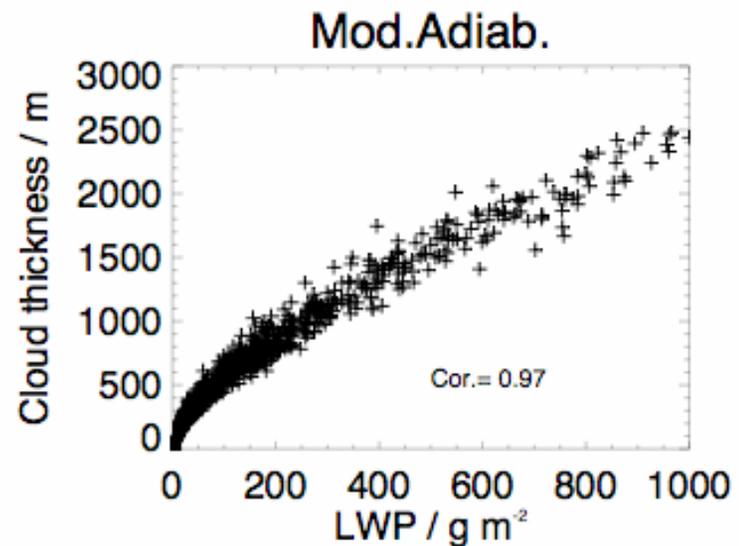
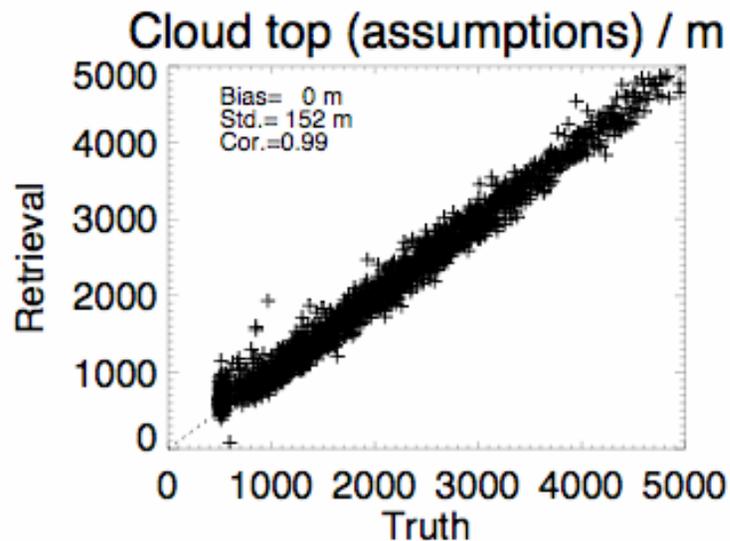
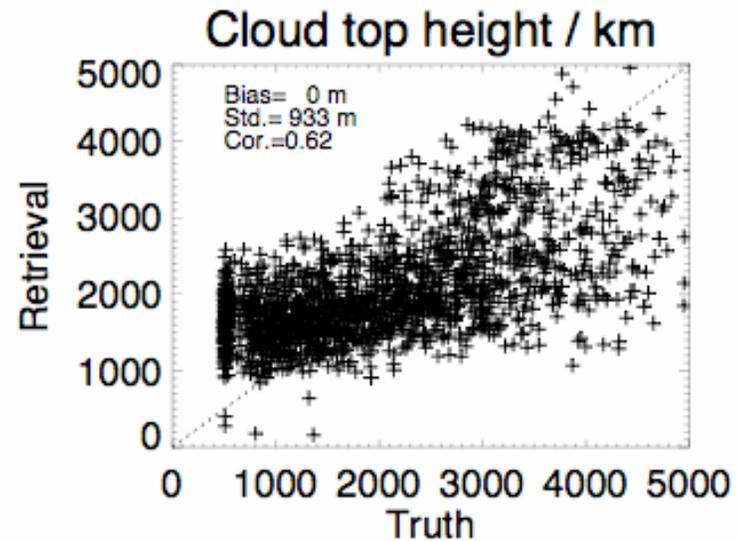
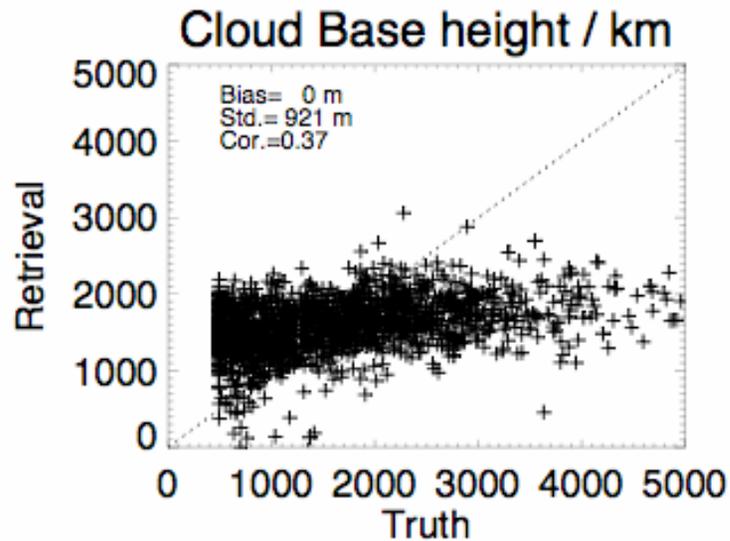


Number of independent pieces of info on LWC(z) is ~1.0 on this more typical cloud; even 90/150 obs don't really help

# Conclusions

- Results assumed CBH and CTH of a single layer cloud is known, forward model is perfect, radiometer uncertainties are uncorrelated and are 0.5 K / channel
- Only under very ideal situations of thick cloud with large LWP are there more than  $\sim 1.1$  DoF for signal
  - These clouds don't exist very often
  - These clouds are often precipitating
- In general, there is only  **$\sim 1$  piece** of information in passive zenith microwave observations between 20-31 GHz on LWC(z)
  - Addition of higher frequencies provides a little more information, but not significant improvement
  - Need to add additional information via scanning with multiple radiometers or with active remote sensors to get LWC(z)

# Aside: Retrieving CBH and CTH



# Large Uncertainties in Retrieved Cloud Thickness

